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Modelling Propagation in Multi-Floor Buildings using the FDTD Method

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Abstract - A three-dimensional parallel implementation of the FDTD method has been used to identify and isolate the dominant propagation mechanisms in a multi-storey building at 1.0 GHz. A novel method to visualise energy flow by computing streamlines of the Poynting vector has been developed and used to determine the dominant propagation mechanisms within the building. It is found that the propagation mechanisms depend on the level of internal clutter modelled. Including metallic and lossy dielectric clutter in the environment increases attenuation on some propagation paths, thereby altering the dominant mechanisms observed. This causes increases in the sector-averaged path-loss and changes the distance-dependency exponents across a floor from 2.2 to 2.7. The clutter also reduces Rician K-factors across the floor. Directly comparing sector-averaged path-loss from the FDTD simulations with experimental measurements shows an RMS error of 14.4 dB when clutter is ignored. However, this is reduced to 10.5 dB when the clutter is included, suggesting that the effects of clutter should not be neglected when modelling propagation indoors.

Index Terms—Finite difference methods, indoor radio communication, modeling, numerical analysis.

I. INTRODUCTION

THE increasing demand for wireless communication services has necessitated the reuse of frequency spectrum. Frequency reuse causes co-channel interference, which is detrimental to system performance, reducing the coverage area, reliability, throughput and the number of users that can be supported [1]. Characterising and mitigating co-channel interference in unlicensed bands remains a major challenge. Indoor systems are particularly susceptible as all transceivers are usually located in close physical proximity. Accurately predicting system performance depends heavily on correctly characterising the indoor propagation environment and a number of models to accurately and reliably predict signal strengths inside buildings have been proposed. Empirical models based on experimental measurements are often used, as the large variability in architectural styles and building materials can complicate deterministic modelling.

Empirical models typically use an exponential distance dependency to predict local means as a function of distance from the transmitter [2], [3]. Shadowing and fading are accounted for by including statistical variation around the local mean prediction [1]. However, empirically-based models cannot explain the physical observations and are thus hard to generalise. For example, many of the terms and parameters in these models lack an electromagnetic basis, and vary considerably between buildings [1], [2]. Consequently, the applicability of empirical models in buildings where measurements were not taken remains a concern. When used in practice, empirical models have been found to result in pessimistic estimates of system performance [1]. More accurate findings have been reported when the empirical models were complemented with physical factors, such as correlated shadowing [1].

Site-specific ray-tracing methods—such as Geometrical Optics (GO) and the Uniform Theory of Diffraction (UTD) have also been widely applied to model propagation within buildings [4]. However, ray methods must be applied to the indoor propagation problem with caution, as many of the assumptions and approximations used in their derivation are not valid for typical indoor environments. For example, structural corners made from lossy dielectric materials (such as concrete) are frequently encountered in indoor environments, however dielectric wedge diffraction is known to be a non rayoptical process [5]. Correctly predicting the diffracted fields is important, as in some circumstances (e.g. deeply shadowed regions) the received power is dominated by diffracted components [6].

The relatively compact size of the indoor propagation problem, and advances in computational technology, are allowing the application of grid-based numerical techniques, such as the Finite-Difference Time-Domain (FDTD) method. Unlike ray-based methods, the FDTD technique does not make a priori assumptions about the propagation processes. Due to the high computational requirements of the FDTD method, previous studies have limited analysis to propagation on two-dimensional TM_z or TE_z horizontal 'slices' through the geometry [6]-[11]. However, two-dimensional results on a horizontal slice may fail to capture propagation mechanisms caused by interactions with the floor or ceiling and cannot be directly verified against experimental measurements. In practical indoor wireless communication systems, frequency channels are often reused between floors in a building, so characterising inter-floor propagation is important to predict the levels of co-channel interference [1]. It is important to note that, unlike the single-floor case, no single two-dimensional slice through a multi-floor geometry can correctly account for all possible propagation paths. For example, many buildings have concrete shafts containing elevators and stairwells, and propagation to adjacent floors around (or through) such shafts can only be thoroughly examined in three-dimensions. For this reason, we regard a three-dimensional characterisation of

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fundamental importance.

Although a three-dimensional characterisation of the propagating fields using the FDTD method is useful, it is the identification and isolation of the dominant propagation mechanisms that is arguably more important-especially for system planners [12]. Specifically, the FDTD simulations can be used to determine which components are important to predict the sector-averaged mean, and which can be reliably ignored. One of the original contributions of this work is the identification (via a rigorous FDTD analysis) of the dominant propagation mechanisms, which could be incorporated into the development of accurate, yet efficient models, suitable for use by system planners on a day-to-day basis. In particular, this paper focuses on providing an independent deterministic validation of the Seidel model [2], and is underpinned with experimental measurements. (This is consistent with the philosophy adopted by Walfisch and Bertoni-in their characterisation of macrocellular systems-who were able to deterministically explain (using Fresnel-Kirchhoff diffraction theory) the $\frac{1}{d^4}$ distance dependency of received power [13], which until then only had an experimental basis [14]).

A further contribution of this paper is an assessment of the impact of clutter in the environment (such as office furniture) on the dominant propagation mechanisms. Interestingly, most existing applications of time-domain methods to model propagation within buildings have assumed these buildings to be empty [6]–[11], [15]–[17] (though [11], [16], [17] did assess the impact of different wall types). However, actual office buildings contain varying amounts of furniture and other metallic and dielectric clutter. In this paper comparisons are made between a basic FDTD model (with a similar level of detail to models in the existing literature) and a more detailed model that includes some furniture and similar objects. Unlike many previous FDTD characterisations of the indoor radio channel, the findings reported in this paper are validated against independent experimental measurements of the pathloss and fading distributions.

A description of the FDTD models is presented in Section II. Section III describes a method of visualising the energy flow by tracing streamlines through the Poynting vector. Section IV presents the simulation results for propagation to the same and adjacent floors. Section V proposes models for the sector-averaged path-loss, while Section VI focuses on the statistical distributions characterising multipath fading. Also considered in Sections IV–VI are the effects of increasing the level of detail in the simulation models and comparisons against experimental measurements. Section VII briefly summarises the findings.

II. PROPAGATION MODELLING WITH THE FDTD METHOD

The building under investigation is the Engineering Tower at The University of Auckland. This is a typical eight-floor 1960's concrete slab building with a services shaft (containing elevators and stairwell) in the centre; in this paper three floors have been considered. The nominal values for the material properties used in FDTD simulation models are: Concrete: $\epsilon_r = 4.0, \sigma = 50$ mS/m; Glass: $\epsilon_r = 3.0, \sigma = 2.0$ mS/m; Drywall: $\epsilon_r = 2.0$, $\sigma = 2.0$ mS/m; Wood: $\epsilon_r = 3.0$, $\sigma = 10$ mS/m; and metal: $\epsilon_r = 1$, $\sigma = 10^7$ S/m. The effects of internal detail/clutter are examined by considering two interior geometries, hereafter referred to as *basic* and *detailed*. The 0.20 m thick concrete floors, 1 cm thick exterior glass and the hollow concrete services shaft are common to both models.

The basic geometry adds internal walls (modelled as 4 cm solid slabs of drywall) creating a corridor around the shaft and dividing the remaining space into nine offices. The detailed geometry models the internal walls as two 1 cm sheets of drywall (separated by a 4 cm air-gap) attached to wooden frames with studs spaced 1.5 m apart. Against each wall, metal bookcases extend floor-ceiling—these contain books, modelled as 0.20 m thick wooden slabs. Doors into the offices and shaft are modelled as wood, and extend slightly into the corridor; the elevator doors are inset and modelled as metal. Metal reinforcing bars (2 cm square) are embedded in the concrete floors on a 1 m² grid, and metal window frames (2 cm square) are spaced 1.5 m apart on the external glass windows. Two flights of concrete stairs are also included in the central shaft.

A single E_z field component is excited with a modulated Gaussian pulse, given by $p(t) = \exp\left[-\left(\frac{t-t_0}{t_w}\right)^2\right] \sin\left(2\pi f_0 t\right)$ with parameters: $f_0 = 1.0$ GHz, $t_w = 1.25$ ns and $t_0 = 5t_w$. This produces a pulse with a 150 MHz 3-dB bandwidth centred around 1.0 GHz. The time step is 18.3 ps. A square lattice size of $\Delta = 1$ cm is used to minimise numerical dispersion [18, pp. 110–128]. The FDTD simulation domain is $18 \times 18 \times 9$ m and is surrounded by a 12-cell thick convolutional perfectly matched layer (CPML) [18, pp. 294–310], resulting in approximately 3 billion mesh cells. Solving this problem using a single processor is not currently feasible and accordingly, the lattice is subdivided and allocated to multiple processors. Field values on the boundaries are exchanged every time step using an implementation of the Message Passing Interface [19]. On a 64-node computer cluster (using Intel Xeon 2.66 GHz processors) these problems require approximately 180 GB of memory and take 48 hours to solve to steady-state (15,000 time steps).

The steady-state electric and magnetic field magnitude and phase were extracted by multiplying the time-series with a 1.0 GHz cissoid. To compare the FDTD results against experimental measurements, the steady-state fields were converted to path-loss (in dB). The radiation pattern from a single E_z component is isotropic in the azimuth plane and proportional to $\sin \theta$ in the elevation plane (i.e. similar to a short dipole antenna). The steady-state E_z fields (in the radial direction) can be converted to path-loss by normalising the values to the Friis equation.

III. VISUALISING ENERGY FLOW

The time-averaged Poynting vector is given by

$$\mathbf{S} = \frac{1}{2} \Re[\mathbf{E} \times \mathbf{H}^*] \quad Wm^{-2}, \tag{1}$$

where \mathbf{E} and \mathbf{H} are the steady-state vector electric and magnetic fields respectively, and * denotes the complex conjugate. At each point in the field, the Poynting vector indicates

the direction and magnitude of energy flow. Streamlines are projected through this space by applying principles developed in fluid dynamics for studying steady flows [20]. (A similar analysis using Poynting vector streamlines to visualise energy flow escaping backwards from a pyramidal horn antenna was reported in [21].)

The local tangent to a streamline is the vector representing energy flow at that point, and in three-dimensions the differential equation governing a streamline is given by

$$\frac{d\vec{p}(a)}{da} = \mathbf{S}(\vec{p}(a)),\tag{2}$$

where \vec{p} is the position, a is the parameter along the streamline, and $\mathbf{S}(\vec{p})$ is the Poynting vector at \vec{p} . Starting from an appropriate initial position, $\vec{p}(a)$, the streamline is computed by numerically solving (2) using forward differences (tracing the direction of the physical propagation of the Poynting vector out of the lattice) or backward differences (tracing the Poynting vector back to the transmitting antenna). The forward difference expression is given by

$$\frac{\vec{p}(a+\bar{a})-\vec{p}(a)}{\bar{a}} = \mathbf{S}(\vec{p}(a)).$$
(3)

A step size $\bar{a} = 2\Delta$ (where Δ is the lattice cell size) was found to be a good trade off between computational efficiency and accuracy. In the case where $S(\vec{p}(a + \bar{a}))$ does not lie on the down-sampled FDTD lattice, it is interpolated using values from adjacent cells. Linear interpolation was found to provide an adequate result. It should be noted that a single initial position results in one streamline which may not be representative of the dominant propagation mechanism in a region. To assist in the visualisation of the net energy flow in a region of space 100 points in a 3λ 'cloud' around the specified initial position are typically seeded.

IV. PROPAGATION MECHANISMS

A. Propagation on the Same Floor

Fig. 1(a) and (b) plot the path-loss on horizontal slices through the basic and detailed internal geometries. The slices are positioned 1.50 m from the floor, in the plane of the transmitting antenna (located at \times). Fig. 2(a) and (b) show streamlines (I–IV) of energy flow, calculated using (3) for both internal geometries. Initial points (\circ) were selected, such that streamlines I and III are shadowed by the central shaft, and II and IV are separated from the transmitter by soft partitions. The central services shaft is observed to significantly shadow waves propagating across the floor when the transmitters are diagonally positioned. Paths penetrating through the shaft are highly attenuated by the thick lossy concrete walls, and consequently, signals received in the shadowed regions are dominated by paths propagating around the shaft.

Energy reaching the shadowed regions in the basic geometry is observed to penetrate through the soft partitioned offices and reflects off the exterior glass windows. This is supported in both Fig. 1(a) and Fig. 2(a), where strong specular reflections from the glass are visible (e.g. streamlines I and II). The presence of strong reflected paths agrees well with previous two-dimensional FDTD simulations of empty buildings [6],





Fig. 1. FDTD simulated path-loss (at 1.0 GHz) on a horizontal slice through the first floor for: (a) basic internal geometry, and (b) detailed internal geometry. The location of the transmitter is indicated by \times , with the floor plan of the building superimposed.

[7], [10]. The problem is nominally symmetric and reflections from both sides of the building contribute equal amounts of power; the resulting $(3\lambda)^3$ sector-averaged path-loss in the shadowed regions is approximately 65 dB.

Comparing Fig. 1(a) with 1(b) and Fig. 2(a) with 2(b) shows a distinct change in the propagation mechanisms, namely strong reflected paths from the windows and drywall are no longer visible. When shelves and books are included against the internal walls, the reflected paths are attenuated to such an extent that (in this case) diffraction around the corners of the concrete shaft is observed to dominate propagation into the shadow regions. Paths involving diffraction exist in the basic geometry, but contribute a small proportion of the total received power. The inclusion of metal window frames also perturbs specular reflection from the glass. The sector averaged path-loss recorded in shadowed regions is up to 15 dB higher than the basic geometry. The attenuation introduced by a single layer of clutter in the environment only slightly reduces the





Fig. 2. Streamlines of energy flow through the single floor environment: (a) basic geometry and (b) detailed geometry. Seed points are marked with \circ . Four seed points (I–IV) are identified for each case.

Fig. 3. FDTD simulated path-loss (detailed geometry at 1.0 GHz) for (a) one floor separating the transmitter and receiver, and (b) two floors separation. The location of the transmitter is indicated by \times .

received power. However, the accumulation of many such effects has the potential to cast significant radio shadows, and may result in other propagation mechanisms dominating. Clutter in the detailed geometry is also observed to introduce strong multi-path components when propagating through the walls, e.g. streamlines II and IV in Fig. 2(a) and (b). This behaviour also alters the fading distributions, and is discussed in further detail in Section VI.

For both the basic and detailed internal geometries, corridors have been modelled as largely clutter free. The sides of the corridor can be considered electrically smooth, and thus the corridor has potential to act as an over-moded waveguide. This mechanism has previously been observed experimentally for relatively long (> 30 m) corridors [22]. In our simulations, the 3λ sector average pathloss is observed to increase from 30 dB to 47 dB when moving 1.5–8.5 m away from the antenna, along the corridor. These values are between 3– 5 dB lower than expected for free-space and are attributed to the reflections from the walls, ceiling and floor. At longer distances the angle of incidence becomes increasingly glancing and it is likely true waveguide modes may be formed.

B. Propagation to Adjacent Floors

Fig. 3 shows the path-loss on horizontal slices (a) one floor and (b) two floors above the transmitter for the detailed geometry (similar to Fig. 1, the slices are positioned 1.5 m above each floor). Comparing the distribution of path-loss one and two floors above the transmitter, Fig. 3(a) and (b), with the same floor case, Fig. 1(b), shows many similarities. In particular, the radio shadow cast by the shaft remains a dominant feature of the indoor environment, and propagation into the shadowed regions remains governed by diffraction at the corners of the shaft. Similar observations can be made for the basic geometry. Clutter in the environment is also observed to introduce strong local shadowing and multi-path. These results suggest that many of the mechanisms identified



Fig. 4. (a) Vertical slice through the three-floor detailed geometry (along - - - indicated in Fig. 3(a)) (b) Poynting vector streamlines on the vertical slice for seed points located on the adjacent floors. (c) Streamline visualisations of propagation paths (from floor 1 to 3) that travel through the shaft.

in the same floor case still dominate propagation to adjacent floors. However, it is noted that the attenuation introduced by each floor is not constant and varies depending on the location of the receiver.

Fig. 4(a) shows the path-loss on a vertical 'slice' through the three-floor detailed geometry; the location of the slice is indicated by - - - in Fig. 3(a). The radiation pattern of the short dipole antenna (located at \times) causes greater pathloss in regions above the antenna. The lower path-loss around point 'A' can be attributed to reflection and scattering from the metal elevator doors. The metal rebar is observed to introduce local scattering, supporting the findings of [23], which showed greater multi-path is present when the rebar embedded in the concrete is included in the analysis. However, the dominant propagation path—penetration through the concrete—remains largely unchanged. Fig. 4(b) shows streamline visualisations of the Poynting vector for four seed points (indicated by \circ , and centred on the vertical slice) located one and two floors above the transmitter. These streamlines largely follow line-ofsight (LOS) paths (though refraction is also visible at the airconcrete and concrete-air interfaces), indicating the dominant propagation mechanism (in this region) is penetration through the floors.

As more floors separate the transceivers, alternative propagation paths involving the lift-shafts and stairwells may contribute significant amounts of power, and may explain the variations in attenuation across each floor. Results indicate these paths are not dominant for a single floor separation. However, as indicated in Fig. 4(c), propagation into the liftshaft can provide a comparable level of power two floors above the transmitter. (Streamline visualisations of the Poynting vector show the net energy flow, and for both paths to be present they have to contribute roughly equal power.) As the walls of the shaft are thicker than the floors, these paths are only visible after two floor penetrations. If the geometry was extended to four floors, paths propagating through the shaft would be expected to dominate the received signal. It should also be noted that, depending on the environment, propagation mechanisms external to the building perimeter may dominate the received power on other floors. Diffraction at a floor/window edge [24] and reflections from surrounding buildings [15] are two such examples.

V. PATH-LOSS PREDICTION MODELS

Fig. 5 shows scatter plots of $(3\lambda)^3$ sector-averaged pathloss (in dB) versus the transmitter-receiver separation distance. Only E_z field points from material-free regions are included in the sector-average. Higher path losses are observed in the detailed geometry, particularly on longer paths. Based on the results presented in Section IV, the change in propagation mechanism from reflection at the glass windows to diffraction at the concrete corner is responsible for the increased pathloss. Also evident in Fig. 5 are a number of sectors (in both geometries) with distance dependency exponents n < 2.0. These sectors occur in the corridors and are caused by strong reflections from the walls, ceiling and floor. Similar observations have been made in [7].

Similar to [2] models in the form d^n are used to relate the average path-loss with the transmitter-receiver separation distance

$$PL(d) = PL(d_0) + 10 \times n_{\rm sf} \times \log_{10}\left(\frac{d}{d_0}\right) + \sum_{f=1}^F {\rm FAF}_f \quad (dB),$$
(4)

where n_{sf} is the distance dependency exponent for data collected on the same floor as the transmitter, $PL(d_0)$ is the path-loss at reference distance $d_0 = 1.0 \text{ m}$, d is the transmitter-receiver separation distance, FAF_f is the floor attenuation encountered propagating through the f^{th} floor, and F is the number of floor separations considered. The parameters n and FAF_f are found by fitting (4) to the data via linear regression, given $PL(d_0 = 1 \text{ m}) = 32.4 \text{ dB}$.



Fig. 5. Scatter plots of $(3\lambda)^3$ path-loss versus distance for (a) basic and (b) detailed internal geometries. The solid lines represent a Seidel model [2] fitted to the simulated data.

TABLE I PARAMETERS FOR THE SEIDEL MODEL [2].

		Basic Geometry	Detailed Geometry	Exper. Meas.
All Regions	$n_{ m sf}$	2.2	2.7	3.6
	FAF_1 (dB)	12.6	12.0	11.8
	FAF_2 (dB)	9.8	10.7	11.0
	RMS error (dB)	5.3	6.5	7.4
Lit Regions	n_{lit}	1.9	2.3	2.9
	FAF_1 (dB)	11.8	11.9	14.6
	FAF_2 (dB)	11.0	12.1	14.2
	RMS error (dB)	3.0	4.4	6.1
Shadowed Regions	$n_{shadowed}$	2.6	3.2	4.2
	FAF_1 (dB)	15.3	14.1	9.0
	FAF_2 (dB)	8.3	8.9	6.6
	RMS error (dB)	3.6	4.1	4.8

Table I shows the least-squares best-fit distance dependency exponents, floor attenuation factors and RMS error between (4) and the FDTD and experimental data. The data collected across the floor has been divided into two regions, lit and shadowed, based on the position of the receiver relative to the transmitter and the concrete services shaft. When all regions are considered, the same floor distance dependency exponent increases for the detailed model due to increased attenuation through the clutter. The increase in RMS error for the detailed geometry also indicates scattering off the clutter introduces greater variability around (4). It is also observed that $FAF_2 < FAF_1$ for both geometries and the experimental measurements. If the only propagation path was through the floors, and if the floors were identical, $FAF_1 = FAF_2$, however, the observed decrease is between 1-3 dB. In other buildings, a greater decrease in the FAF is observed (e.g. $FAF_1 = 12.9 \text{ dB}$ and $FAF_2 = 5.8 \text{ dB}$ [2]), and this behaviour is difficult to explain experimentally [2].

As shown in Fig. 4(b), penetration through the floors is the dominant propagation mechanism in the lit regions (for both internal geometries), and consequently $FAF_1 \approx FAF_2$. In the basic geometry $n_{lit} = 1.9$, which is close to free-space (n = 2.0). The streamline visualisations of the Poynting vector presented in section IV-A show the dominant propagation path in lit regions is largely LOS. The soft partitions do not perturb the propagating waves or introduce appreciable attenuation. However, in the detailed geometry $n_{lit} = 2.3$, which tends to indicate clutter in the environment introduces additional attenuation. This is also supported by examining streamlines II and IV in Fig. 2(b), which show the energy tends to propagate on non-LOS paths in the lit regions. The streamlines presented in Fig. 4(c) indicate other (lower-loss) propagation paths may dominate in the shadowed region. It is thought the presence of such paths is (partly) responsible for the decrease in FAF between one and two floor separations. It is noted that $n_{shadowed} > n_{lit}$ for both geometries and experimental measurements.

Comparisons with Experimental Measurements

To confirm the findings made with the FDTD method, experimental measurements were conducted at 1.8 GHz over two floors of the Engineering building. Similar to [1], the transmitter carrier frequencies were spaced 400 kHz apart allowing the power received from transmitters located on adjacent floors to be measured in a single sweep. Identical, vertically orientated, discone antennas were used in both transmitter and receiver, and located approximately 1.6 m from the floor. The radiation pattern of the discone antennas is isotropic in the azimuth plane and the gain was calculated from test measurements in an anechoic chamber. 52 measurements were made across the floor and the receiving antenna was rotated over a 1 m diameter locus to average out the effects of multipath fading. The voltage envelope was also recorded and used to determine the fading distributions.

As the relevant material properties do not change significantly over the 1.0–1.8 GHz frequency range [3], a direct comparison between the path-loss for 1.0 GHz FDTD simulations and 1.8 GHz experimental measurements only needs



Fig. 6. Scatter plot comparing sector-averaged measurements of the pathloss with values obtained from FDTD simulations in the same locations. Both basic and detailed internal geometries have been considered, and in both cases the FDTD method generally underestimates the sector-averaged path-loss.

to account for the increased free-space loss (5.1 dB). Fig. 6 shows a point-wise comparison between the average path-loss recorded for the 104 experimental data points, and $(3\lambda)^3$ sector averaged FDTD simulations of the path-loss made at the same locations. It is noted that the FDTD simulations underestimate the path-loss for many sectors. This underestimation cannot be accounted for in the frequency difference; and is largest in regions furthest from the transmitter (and on highly cluttered paths) particularly paths shadowed by the shaft or passing through multiple partitions. Adding internal clutter improves the prediction accuracy, as shown in Fig. 6 the RMS error between the measurements and simulation is 14.4 dB for the basic geometry; this is reduced to 10.5 dB when the clutter is included. This result is significant, as it suggested that to correctly predict the path-loss, clutter present in the indoor propagation environment must be considered when applying full-wave electromagnetic methods. Although further environmental details/clutter could be added to improve the accuracy of the FDTD predictions, the random nature of the clutter (e.g. size, position and properties) complicates a fullydeterministic characterisation of the indoor radio channel.

VI. FADING DISTRIBUTIONS

Rayleigh and Rician distributions are frequently used to characterise multipath fading for indoor environments [1]. When a specular component is stronger than the scattered components—for example, on a line-of-sight (LOS) path—the probability density function (PDF) of the signal envelope follows a Rician distribution, given by

$$f(x) = \frac{x}{\sigma^2} \exp\left(\frac{-x^2 + s^2}{2\sigma^2}\right) I_0\left(\frac{xs}{\sigma^2}\right),$$
 (5)

where s^2 is the power of the dominant component, $2\sigma^2$ is the mean scattered power, and I_0 is the zero-th order Bessel function of the first kind. The Rician *K*-factor is defined as



Fig. 7. Cumulative distribution functions of the received power envelope (in dB) normalised to the path-loss for both internal geometries and experimental measurements compared with exact Rician distributions. The E_z field data was recorded in the shaded regions on the same floor as the transmitter (located at \times).

the ratio of specular power to scattered power, $K = \frac{s^2}{2\sigma^2}$, and is determined from the FDTD simulated data using [25]

$$\frac{\mathrm{E}\left[x\right]}{\sqrt{\mathrm{E}\left[x^{2}\right]}} = \sqrt{\frac{\pi}{4(K+1)}} \exp\left(-\frac{K}{2}\right) \\ \times \left[(1+K)I_{0}\left(\frac{K}{2}\right) + KI_{1}\left(\frac{K}{2}\right)\right], \tag{6}$$

where $E[x^2]$ is the average square amplitude, E[x] is the average amplitude, and I_m is the *m*-th order Bessel function of the first kind. In the case where no single component dominates (K = 0), the PDF of the signal envelope follows a Rayleigh distribution, given by

$$f(x) = \frac{x}{\sigma^2} \exp\left(\frac{-x^2}{2\sigma^2}\right),\tag{7}$$

where σ^2 is the mean power.

Fig. 7 shows cumulative distribution functions (CDF) of received signal envelope (in dB) normalised to the mean path-loss for both internal geometries and experimental measurements. Also shown in Fig. 7 is a floor plan; the data was collected in the shaded sectors—located within an office, approximately 5 m from the transmitter. Rician distributions are fitted to these data sets using (6). In the basic geometry K is 2.6—this indicates a strong dominant component exists whereas, in the detailed geometry and measurements K = 0, suggesting more energy is being scattered in this case. The experimental data set consists of 400 points, whereas the simulated data set has 2.5×10^5 points. Consequently, there is a greater variability between the experimental and theoretical CDFs, particularly at lower signal powers.

The differences in Rician K-factor for the basic and detailed geometries can be explained by examining streamline visualisations of the Poynting vector. Fig. 8 shows streamlines for the (a) basic; and (b) detailed geometries, reaching the same sectors considered in Fig. 7. In the basic geometry it is



Fig. 8. Streamline visualisations of the Poynting vector traced from seed points (located in the shaded region in Fig. 7) to the transmitting antenna for (a) basic and (b) detailed internal geometries.

observed that the energy is travelling on the LOS path with some attenuation when penetrating through the soft partitions; accordingly, K is greater than zero. The same streamline in the detailed geometry shows the LOS path is blocked by book-shelves. The increased attenuation allows additional scattered paths (of similar magnitude to the attenuated-LOS path) to exist and accordingly, the PDF of the signal envelop follows a Rayleigh distribution. Similar phenomena are observed in other locations shadowed by clutter.

VII. CONCLUSIONS

A three-dimensional parallel FDTD algorithm has been used to identify and isolate the dominant propagation mechanisms in a multi-storey building. A simplified model based on the dominant mechanisms has been compared against experimental measurements of the path-loss. Streamline projections through the Poynting vector show that the dominant propagation mechanisms can change significantly when metallic and lossy dielectric clutter is included (the clutter also reduces Rician K-factors across the floor). The change in propagation mechanisms results in a lower RMS error when the FDTD simulation results are compared with measurements.

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